Dirichlet forms on canonically compactifiable graphs

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ABSTRACT. We consider weighted graphs with an infinite set X of vertices, such that every function of finite energy is bounded. For each of these graphs there is a compact set K containing X as a dense subset and we can define some kind of boundary as $\partial X := K \setminus X$. We then equip the graphs with a finite measure and define two natural Dirichlet forms, $Q^{(D)}$ and $Q^{(N)}$, which we refer to as the forms with Dirichlet and Neumann boundary conditions, respectively. We proof that every form Q, such that $Q^{(N)} \leq Q \leq Q^{(D)}$, can be decomposed into a part living on X and a part living on ∂X . We show, that the part living on the boundary is a Dirichlet form with respect to a certain measure.